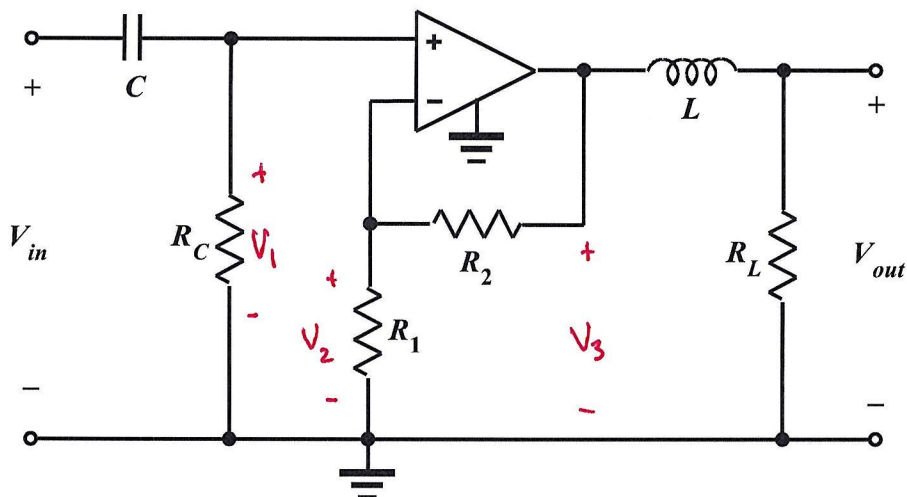


Homework Problem #026

- a. For the active filter circuit shown below, determine an expression for the voltage transfer function in terms of C , R_C , R_1 , R_2 , L and R_L .



$$V_{out} = \frac{R_L}{R_L + j\omega L} V_3, \quad V_3 = \left(1 + \frac{R_2}{R_1}\right) V_2, \quad V_2 = V_1, \quad V_1 = \frac{R_C}{R_C + \frac{1}{j\omega C}} V_{in}$$

$$\therefore \frac{V_{out}}{V_{in}} = \left(\frac{R_L}{R_L + j\omega L}\right) \left(1 + \frac{R_2}{R_1}\right) \left(\frac{R_C}{R_C + \frac{1}{j\omega C}}\right)$$

- b. Characterize the circuit as BP or BS, and explain your decision.

$$\left| \frac{V_{out}}{V_{in}} \right| = \frac{R_L \left(1 + \frac{R_2}{R_1}\right) R_C}{\sqrt{[R_L^2 + (\omega L)^2] [R_C^2 + (\frac{1}{\omega C})^2]}}$$

$$\lim_{\omega \rightarrow \infty} \left| \frac{V_{out}}{V_{in}} \right| = 0, \quad \lim_{\omega \rightarrow 0} \left| \frac{V_{out}}{V_{in}} \right| = 0, \quad \left| \frac{V_{out}}{V_{in}} \right| \text{ can never be } < 0$$

\therefore This is a Band Pass (BP) filter.

- c. Given $C = 5 \text{ nF}$, $R_C = 100 \text{ k}\Omega$, $R_1 = 10 \text{ k}\Omega$, $R_2 = 90 \text{ k}\Omega$, $L = 1.1 \text{ H}$ and $R_L = 200 \text{ k}\Omega$, use LTspice to verify your claim.

See the attachment.

- d. Use your LTspice plot to estimate the cutoff frequencies for this filter.

The cutoff frequencies are $\approx 300 \text{ Hz}$ and $\approx 20 \text{ kHz}$

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Spring 2022 EE 3340 Homework Problem 26.cir
* Q:\EE 3340\homework problems\26.cir
Vin in 0 AC 1 0
C in 1 5n
RC 1 0 100k
R1 2 0 10k
R2 2 3 90k
E 3 0 2 1 1T
L 3 out 1.1
RL out 0 200k
.AC DEC 10 1m 1g
.end
```

